

62. $X = \text{time (days)}$
 $Y = 37 \sin\left(\frac{2\pi}{365}(X-101)\right) + 25$
 $Y = \text{Temp (ave daily)}$

a) what day is temp increasing fastest (biggest roc)

$Y' = \frac{2\pi}{365} \cdot 37 \cos\left(\frac{2\pi}{365}(X-101)\right)$ max at this when $X=101$

rate of change of temp
 roc
 $Y'(101) = .631 \frac{^\circ}{\text{day}}$

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49. $x = t^2 + t$ $y = \sin t$

a) $\frac{dy}{dx} = \frac{\cos t}{2t+1} \cdot \frac{dt}{dx}$

b) $\frac{d}{dt}\left(\frac{dy}{dx}\right) = \frac{(2t+1)(-\sin t) - \cos t \cdot 2}{(2t+1)^2}$

c) $\frac{d}{dx}\left(\frac{dy}{dx}\right) = \frac{\frac{d}{dt}\left(\frac{dy}{dx}\right)}{\frac{dx}{dt}} = \frac{(2t+1)(-\sin t) - 2\cos t}{(2t+1)^3}$

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3.7a Implicit Differentiation

differentiate: Find $\frac{dy}{dx}$

$y = 1 - x^2$ explicit $\frac{dy}{dx} = -2x$ $\frac{dx}{dy} = 1$

$x^2 + y = 1$ implicit $2x + \frac{dy}{dx} = 0$ $\frac{dy}{dx} = -2x$ $\frac{dy}{dx} = 1$

$y^2 = x$ explicit $y = \sqrt{x} = x^{\frac{1}{2}}$
 $2y \cdot \frac{dy}{dx} = 1$
 $\frac{dy}{dx} = \frac{1}{2y}$
 $\frac{dy}{dx} = \frac{1}{2} x^{-\frac{1}{2}}$
 $= \frac{1}{2} \cdot \frac{1}{x^{\frac{1}{2}}}$
 $= \frac{1}{2\sqrt{x}} = \frac{1}{2y}$

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Find the slope of the circle at the point (3, -4)

$x^2 + y^2 = 25$

$2x + 2y \cdot y' = 0$

$2y \cdot y' = -2x$

$y' = \frac{-2x}{2y} = \frac{-x}{y} \Big|_{(3, -4)} = \frac{-3}{-4} = \frac{3}{4}$

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Implicit Differentiation Process

1. Differentiate both sides of the equation *term by term* with respect to x .
2. Collect the terms with dy/dx on one side of the equation
3. Factor out dy/dx .
4. Solve for dy/dx .

lens, tangents and normal lines

find the tangent and normal lines to the ellipse at the point $(-1, 2)$

$$x^2 - (y-1)^2 + y^2 = 7$$

$$2x - (xy' + y \cdot 1) + 2yy' = 0$$

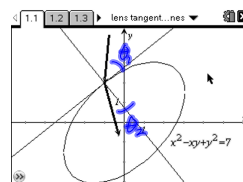
$$2x - xy' - y + 2yy' = 0$$

$$-xy' + 2yy' = -2x + y$$

$$y'(-x + 2y) = -2x + y$$

$$y' = \frac{-2x + y}{-x + 2y} \bigg|_{(-1, 2)} = \frac{2 + 2}{1 + 2 \cdot 2} = \frac{4}{5}$$

$$\text{tan line: } y = \frac{4}{5}(x+1) + 2 \quad \text{normal: } y = -\frac{5}{4}(x+1) + 2$$



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higher order derivatives

Find the second derivative of y with respect to x

$$2x^3 - 3y^2 = 8$$

$$6x^2 - 6yy' = 0$$

$$y' = \frac{-6x^2}{-6y} = \frac{x^2}{y}$$

$$y'' = \frac{y \cdot 2x - x^2 y'}{y^2} = \frac{2xy - x^2 \cdot \frac{x^2}{y}}{y^2} = \frac{2xy^2 - x^4}{y^3}$$

$$y'' = \frac{2xy^2 - x^4}{y^3}$$

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